

Part 1: Data Sc	sience \equiv information compression & expansion
□ Complex-time	(<i>KIME</i>) & rationale
□ Solutions of ul	trahyperbolic wave equations
Open spaceki	me problems
Data science a	applications
Bayesian form	ulation of spacekime inference
Part 2: HDDA -	Spacekime Events (Skevents)
🖵 Part 3: Applicat	tions Spacekime Analytics Tutorial (Demos)

Duality of Evidence-based Scientific Discovery experimental → theoretical → computational → data sciences				
<u>Mapping</u> Examples	<u>Analysis</u> Observables/Data → Compact Models	$\frac{Synthesis}{Compact Models \rightarrow}$ (simulated, actionable info)		
1. <i>Lossless</i> Math Transforms	(A.1.1) <u>Linear transform</u> , L: $V \to W$, e.g., 2D rigid body $L = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} : \mathbb{R}^2 \xrightarrow{rotation} \mathbb{R}^2$ (A.1.2) <u>Fourier transform</u> : $\hat{f}(\omega) = \int_{-\infty}^{\infty} f(x) e^{-i2\pi\omega} dx$	(5.1.1) <u>Inverse linear transform</u> , $L^{-1}: W \to V$, e.g., $L^{-1} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} : \mathbb{R}^2 \xrightarrow{rotation} \mathbb{R}^2, LL^{-1} \equiv \mathbb{I}$ (5.1.2) <u>Inverse Fourier (IFT)</u> : $f(x) = \int_{-\infty}^{\infty} \hat{f}(\omega) e^{i2\pi\omega x} d\omega$		
2. DNA	(A.2.1) <u>DNA Packing</u> in Chromatin Fiber Chromosomes contain enormously long linear DNA molecules associated with proteins that fold and pack the fine DNA double helix into a <i>tight compact structure</i>	(S.2.1) <u>DNA Unpacking</u> The process of unfolding the DNA from the chromosome to support the processes of <u>gene expression</u> , <u>DNA replication</u> , and <u>DNA repair</u>		
3. <i>Lossy</i> Data/Stats Science	(A.3.1) Info Compression, e.g., linear models Y = 4582.70 + 212.29 X Data $\xrightarrow{assumption} Model$	(S.3.1) Information Inflation, Simulation & Generation, e.g., forecasting, regression, interpolation, extrapolation (predict & classify new data): Input $\xrightarrow{model} Output$		
4. Artificial & Augmented Intelligence	$\begin{array}{c} (A.4.1) \\ \underline{Building, Fitting \& Training} \\ large foundational, generative \\ \& deep network AI models \\ \underline{Data} \xrightarrow{human+infrastructur} GAIM \\ \hline \end{array}$	$\begin{array}{c c} (S.4.1) \text{ Generative Artificial} \\ Intelligence Modeling (GAIM) \\ Human Prompt \stackrel{GAIM}{\longrightarrow} Result \end{array} \xrightarrow{\text{COCHABE for local contents}} \begin{array}{c c} COCHABE for local contents \\ \hline \hline \\ \hline $		
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AI & Spacekime Analytics

<u>Rationale for *Time* \Rightarrow *Kime* Extension</u>

<u>Math</u> – *Time* is a special case of *kime*, $\kappa = |\kappa|e^{i\varphi}$ where $\varphi = 0$ Time (\mathbb{R}^+) is a subgroup of the multiplicative Reals group Whereas <u>kime</u> (\mathbb{C}) is an algebraically *closed prime field* that naturally extends time

Time is ordered but kime is not!

Kime (\mathbb{C}) represents the smallest natural extension of time, as a complete filed that agrees with time

Physics -

- The Problem of Time: Time has different meanings in *quantum mechanics* & general relativity; Hence, a tension in formulating a *Quantum Gravity Theory* unifying the two ... (DOI 10.1007/978-3-319-58848-3)
- R and C Hilbert-space quantum theories make different predictions (DOI: 10.1038/s41586-021-04160-4)

Bio Al/Data Science – Random IID sampling, Bayesian reps, tensor modeling of C kimesurfaces, novel analytics

Wesson (2004, 2010) Dinov & Velev (2021) Wang et al. (2022) Zhang et al. (2023) Dinov & Shen (2024)









Wang et al., 2022 | Dinov & Velev (2021)











(Many) Spacekime Open Math Problems

Ergodicity

Let's look at particle velocities in the 4D Minkowski spacetime (X), a measure space where gas particles move spatially and evolve longitudinally in time. Let $\mu = \mu_x$ be a measure on X, $\underline{f(x, t)} \in L^1(X, \mu)$ be an integrable function (e.g., <u>velocity</u> of a particle), and $\underline{T}: X \to X$ be a measure-preserving transformation at position $x \in \mathbb{R}^3$ and time $t \in \mathbb{R}^+$.

A pointwise ergodic theorem argues that in a measure theoretic sense, the average of f (e.g., velocity) over all particles in the gas system at a fixed time, $\bar{f} = \mathbb{E}_t(f) = \int_{\mathbb{R}^3} f(\mathbf{x}, t) d\mu_{\mathbf{x}}$, will be equal to the average f of just one particle (\mathbf{x}) over the entire time span,

$$\tilde{f} \equiv \mathbb{E}_{x}(f) = \lim_{n \to \infty} \left(\frac{1}{n} \sum_{m=0}^{n} f(T^{m}x) \right)$$
, i.e., (show) $\bar{f} \equiv \tilde{f}$.

The spatial probability measure is denoted by μ_x and the transformation $T^m x$ represents the dynamics (time evolution) of the particle starting with an initial spatial location $T^o x = x$.

Investigate the ergodic properties of various transformations in the 5D spacekime:

$$\underbrace{\bar{f} \equiv \mathbb{E}_{\kappa}(f) = \frac{1}{\mu_{x}(X)} \int f\left(x, \underline{t}, \underline{\phi}\right) d\mu_{x}}_{\text{space averaging}} \stackrel{f}{\cong} \underbrace{\lim_{t \to \infty} \left(\frac{1}{t} \sum_{m=0}^{t} \left(\int_{-\pi}^{+\pi} f(T^{m}x, t, \phi) d\Phi\right)\right) = \mathbb{E}_{x}(f) \equiv \tilde{f}}_{\text{kime averaging}}$$

Dinov & Velev (2021

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Physics	Bio-Data Sciences
A particle is a small localized object that permits	An <u>object</u> is something that exists by itself, actually or
observations and characterization of its physical or	potentially, concretely or abstractly, physically or incorporeal
chemical properties	(e.g., person, subject, etc.)
An observable a dynamic variable about particles that	A (RV) feature is a dynamic variable or an attribute about an
can be measured	object that can be measured
Particle state is an observable particle characteristic	Datum is an observed quantitative or qualitative value, an
(e.g., position, momentum)	instantiation, of a feature
Particle system is a collection of independent particles	Problem, aka Data System, is a collection of independent
and observable characteristics, in a closed system	objects and features, without necessarily being associated with
-	a priori hypotheses
Wave-function	Inference-function
Reference-Frame <u>transforms</u> (e.g., Lorentz)	Data transformations (e.g., wrangling, log-transform)
State of a system is an observed measurement of all	Dataset (data) is an observed instance of a set of datum
particles ~ wavefunction	elements about the problem system, $O = \{X, Y\}$
A particle system is computable if (1) the entire	Computable data object is a very special representation of a
system is logical, consistent, complete and (2) the	dataset which allows direct application of computational
unknown internal states of the system don't influence the	processing, modeling, analytics, or inference based on the
computation (wavefunction, intervals, probabilities, etc.)	observed dataset
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Mathematical-Physics \implies Bio-Data Science & Al			
Physics	Data Science		
<u>Wavefunction</u>	 Inference function - describing a solution to a specific data analytic system (a problem). Examples: A linear (GLM) model represents a solution of a prediction inference problem, Y = Xβ, where the inference function quantifies the effects of all independent features (X) on the dependent outcome (Y), data (X = (X = Y)). 		
Wave equ problem: $\left(\frac{\partial^2}{\partial x^2} - \frac{1}{\nu^2}\frac{\partial^2}{\partial t}\right)\psi(x,t) = 0$	$\psi(0) = \psi(X,Y) \implies \hat{\beta} = \hat{\beta}^{OLS} = \langle X X \rangle^{-1} \langle X Y \rangle = (X^T X)^{-1} X^T Y.$ • A non-parametric, <u>non-linear</u> , alternative inference is SVM classification. If $\psi_x \in H$, is the lifting function $\psi: R^\eta \to R^d$ ($\psi: x \in R^\eta \to \tilde{x} = \psi_x \in H$), where $\eta \ll d$, the kernel $\psi_x(y) = \langle x y \rangle: 0 \times R$ transformes non-linear to linear separation, the observed data $O_i = \{x_i, y_i\} \in R^\eta$ are lifted to a H . The SVM prediction operator is the weighted sum of the kernel functions at ψ_{O_i} , where β^* is a solution to the SVM regularized optimization:		
complex solution: $\psi(x,t) = Ae^{i(kx-wt)}$ represents a traveling wave, where $\left \frac{w}{k}\right = v$.	$\begin{split} \underbrace{\langle \psi_0 \mid \beta^* \rangle_H}_{predictions} &= w^T x + b = \sum_{i=1}^n p_i^* \langle \psi_0 \mid \psi_{0i} \rangle_H + b, \\ \min_{w \in \mathbb{R}^d, \xi \in \mathbb{R}^+} \begin{pmatrix} regularizer & fidelity \\ \ w\ ^2 &+ C \sum_{i=1}^m \xi_i \end{pmatrix}, y^{(i)} (w^T x^{(i)} + b) \geq 1 - \xi_i, \xi_i \geq 0 \\ \text{The dual weight coefficients, } p_i^*, \text{ are multiplied by the label corresponding to each training instance, } \{y^{(i)}\}. \\ \text{Inference always depends on the (input) data; however, it does not have 1-1 and onto bijective correspondence with the data, since the inference function quantifies predictions probabilistically. \end{split}$		
GLM/SVM: https://DSPA2.predictive.space Dinov, Springer (2018, 2023)			





















Bayesian Inference Simulation

The correlation between the original data (*A*) and its reconstruction using a single kime magnitude and the correct kime-phases (*C*) is $\rho(A, C) = 0.89$.

This strong correlation suggests that a substantial part of the *A* process <u>energy can be recovered using only a</u> <u>single observation</u>. In this case, to reconstruct the signal back into spacetime and compute the corresponding correlation, we used a single kimemagnitude (sample-size=1) and process *C* kimephases.



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Bayesian Inference Simulation

Let's demonstrate the Bayesian inference corresponding to this spacekime data analytic problem using a simulated bimodal experiment:

 $X_A = 0.3U + 0.7V$, where $U \sim N(0,1)$ and $V \sim N(5,3)$

Specifically, we will illustrate the Bayesian inference using repeated single spacetime observations from cohort *A*, $X = \{x_{i_o}\}$, and varying kime-phase priors (φ = phase aggregator) obtained from cohorts *B*, *C*, or *D*, using different posterior predictive distributions.

Relations between the empirical data distribution (<u>dark blue</u>) and samples from the posterior predictive distribution, representing Bayesian simulated spacekime reconstructions (<u>light-blue</u>). The derived Bayesian estimates do not perfectly match the empirical distribution of the simulated data, yet there is clearly information encoding that is captured by the spacekime data reconstructions.

This <u>signal compression</u> can be exploited by subsequent model-based or model-free data analytic strategies for retrospective prediction, prospective forecasting, ML classification, AI derived clustering, and other spacekime inference methods.







Part 2: Example – Quantum Spacekime Entropy

Assume Laplace Phase distribution and Exponential Time

- **Kime-Phase Distribution** $(\Phi(\varphi))$: Laplace distribution μ (location) and scale b, $\Phi(\varphi) = \frac{1}{2b} \exp\left(-\frac{|\varphi-\mu|}{b}\right)$. **Time Distribution** $(p_T(t))$: Exponential decay distribution with parameter λ , $p_T(t) = \lambda e^{-\lambda t}$, $t \ge 0$.
- **Spatial Distribution** $(p_X(X))$: Uniform over a volume *V* in 3D Euclidean space, $p_X(X) = \frac{1}{v}$, for $X \in V$.

The joint probability distribution is $p(\kappa) = p_X(X)p_T(t)\Phi(\varphi) = p(\kappa) = \frac{1}{V}\lambda e^{-\lambda t}\frac{1}{2b}\exp\left(-\frac{|\varphi-\mu|}{b}\right)$. And the quantum entropy is $S_{\kappa} = -(\rho_{\kappa}\log\rho_{\kappa})$. The trace of ρ_{κ} is $\operatorname{Tr}(\rho_{\kappa}) = \sum_{\kappa} \langle \psi(\kappa) | \rho_{\kappa} | \psi(\kappa) \rangle$, subject to normalization condition for probabilities, $\operatorname{Tr}(\rho_{\kappa}) = 1$. Then,

$$\log \rho_{\kappa} = \log \left(\frac{1}{V} \lambda e^{-\lambda t} \frac{1}{2b} \exp \left(-\frac{|\varphi - \mu|}{b} \right) \right) = \log \rho_{\kappa} = \log \left(\frac{\lambda}{2bV} \right) - \lambda t - \frac{|\varphi - \mu|}{b}.$$

$$(\text{discrete}) S_{\kappa} = -\sum_{X} \sum_{T} \sum_{\varphi} \frac{1}{V} \lambda e^{-\lambda t} \frac{1}{2b} \exp \left(-\frac{|\varphi - \mu|}{b} \right) \log \left(\frac{\lambda}{2bV} \right) - \lambda t - \frac{|\varphi - \mu|}{b}.$$

$$(\text{continuous}) S_{\kappa} = \frac{1}{V} \int_{V} \int_{0}^{\infty} \int_{-\infty}^{\infty} \frac{\lambda e^{-\lambda t}}{2b} \exp \left(-\frac{|\varphi - \mu|}{b} \right) \left[\log \left(\frac{\lambda}{2bV} \right) - \lambda t - \frac{|\varphi - \mu|}{b} \right] d\varphi dt dV = -\log \left(\frac{\lambda}{2bV} \right) + \frac{1}{\lambda} + 1.$$

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Part 3: Applications: Spacekime Analytics Tutorial

TCIU/Spacekime Analytics Tutorial: **Basic TCIU Protocol for Predictive Spacekime Analytics using** Longitudinal Data

	SOCR > TOU Website > TOU GetHub >			
1 Preliminary setup				
2 Longitudinal Data Import	Spacekime Analytics (Time Complexity and			
3 Time-series graphs	Information I I in contraints (Information Complexity)			
3.1 Interactive time-series visualization	Interential Uncertainty)			
3.1.1 Example fMRI(x=4, y=42, z=33, t)	Basic TCIU Protocol for Predictive Spacekime Analytics using Longitudinal Data SOCR Team			
4 Kime-series/Kime-surfaces (spacekime analytics protocol)				
4.1 Pseudo-code	05/13/2024			
4.2 Function main step: Time- series to Kime-surfaces Mapping	This Spacekime TCIU Learning Module presents the core elements of spacekime analytics including: • Import of repeated measurement lontitudinal data.			
4.2.1 Generate the kime-phases	Numeric (stitching) and analytic (Laplace) kime-surface reconstruction from time-series data,			
4.2.2 Structural Data Preprocessing	 Forward prediction modeling extrapolating the process behavior beyond the observed time-span (0, T). Group comparison discrimination between cohorts based on the structure and properties of their corresponding kime- surfaces. For instance, statistically quantify the differences between two or more proups. 			
4.2.3 Intensity Data Preprocessing	transportiet duttering and classification of individuals, track, and other latent characteristics of cases included in the study, construct low dimensional visual representations of large repeated measurement data across multiple individuals as por knews surfaces (parametericae) 20 manifolds), statistical comparison and quantitative contrasting of kime surface differences. Preliminary setup			
4.2.4 Generate plotly labels				
4.2.5 Cartesian space interpolation				
4.2.6 Cartesian representation				
4.2.7 Generate a long data- frame	TCIU and other is package dependencies			
4.2.8 Display kime-surfaces	Solw			
4.3 Analytical Time-series to Kime- Surface Transformation (Loplace)	2 Longitudinal Data Import			
	In this case, we are just loading some exemplary fMRI data, which is available here.			



https://www.socr.umich.edu/TCIU/HTMLs/Chapter6 TCIU Basic SpacekimePredictiveAnalytics.html

Available AI Resources SOCR Motto – "It's Online & Freely Accessible, Therefore it Exists!" Pubs: https://socr.umich.edu/people/dinov/publications.html GitHub: https://github.com/SOCR PIPM App: https://rcompute.nursing.umich.edu/PIPM v2/ AI Apps: https://socr.umich.edu/HTML5/ (SOCR AI Bot) Demos: https://DSPA2.predictive.space (Appendix 9 – OpenAI Synth Text Img & Code) Tutorials: https://TCIU.predictive.space & https://SpaceKime.org \square Website: https://socr.umich.edu

